

# Conceptual Questions

1. Ignoring air resistance, the acceleration of a Projectile is vertically downward at all time  $\downarrow -9.81 \frac{m}{s^2}$

2.  $V_y = 0$ , The x component, on the



other hand is always  $v_0 \cos \theta$ .  $\therefore$  the Projectile  $v_{avg}$

3. has magnitude of  $v_0 \cos \theta$  + points in the positive x dir.

7. Less than  $45^\circ$  - see figure 4-9



The Projectile was launched at an angle of  $30^\circ$  above the positive axis; when it landed its direction of motion was  $30^\circ$  below the positive axis hence it change direction was  $60^\circ$  counter clock wise

9. a) from the child point of view of the parents the scoop of ice cream falls straight down B) Parents Point of view Parabolic trajectory

## Conceptual Exercises

1. a) you + the ball have the same horizontal component of velocity  $\therefore$  the ball will come down in your hand.

3. The Divers are in Free fall for the same amount of time. It follows that Diver 2 covers  
b) twice the distance.

5. a) Proj A, B + C

b) Proj C, B, A

6. a)  $A > B > C$  for initial Speed

b)  $A = B = C$

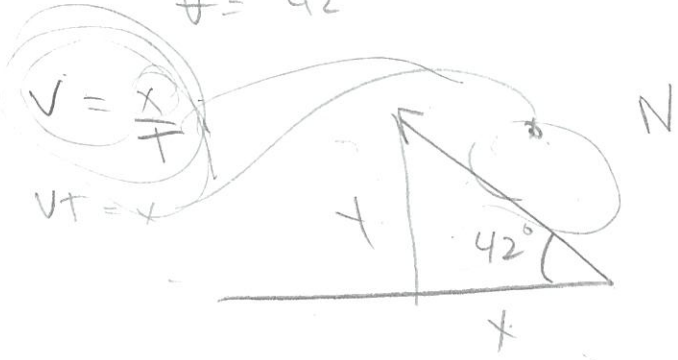
# Sec 4.1

$\Delta x = 4800\text{m}$

1.  $V_i = 3.2 \frac{\text{m}}{\text{s}} \left( \frac{1500\text{s}}{1 \text{min}} \right)$   $t = 25 \text{min} \left( \frac{60\text{s}}{1 \text{min}} \right) = 1500\text{s}$

$\theta = 42^\circ$

$x = v_x t$



a) west =  $-3567\text{m} =$

b) North =  $3210\text{m} =$   
 $y = v_y t$

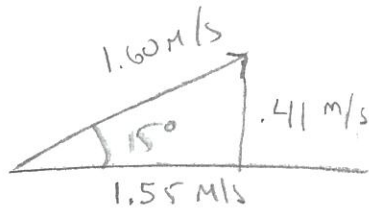
2.  $V_i = 1.60 \frac{\text{m}}{\text{s}}$

$\theta = 15^\circ \text{ N of E}$

$T = ?$

a)  $20\text{m E.}$

b)  $30\text{m N.}$



$1.55 \frac{\text{m}}{\text{s}} = \frac{20\text{m}}{T}$

a)  $T = 12.9\text{s}$

b)  $1.41 \frac{\text{m}}{\text{s}} = \frac{30\text{m}}{T}$

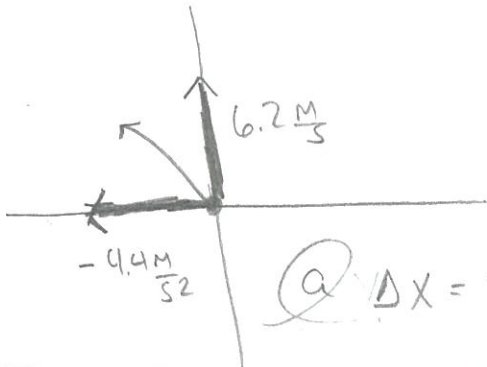
$T = 73.2\text{s}$

4.

$y = 6.2 \text{ m/s}$

$a = -4.4 \frac{\text{m}}{\text{s}^2}$

a)  $T = 5.0\text{s}$



a)  $V = \frac{y}{T} = v T = y$

$= (6.2 \frac{\text{m}}{\text{s}}) (5.0\text{s}) = 31\text{m}$

b)  $V_x = v_{0x} + at$

$= -4.4 \frac{\text{m}}{\text{s}^2} \cdot 5\text{s} = -22 \frac{\text{m}}{\text{s}}$

a)  $\Delta x = v_i t + \frac{1}{2} a t^2$   
 $0 + \frac{1}{2} (-4.4 \text{ m/s}^2) \cdot 5^2 = -55\text{m}$

5.

$v_x = 2.10 \times 10^9 \frac{\text{cm}}{\text{s}}$

$a_T = 5.30 \times 10^{11} \frac{\text{cm}}{\text{s}^2}$

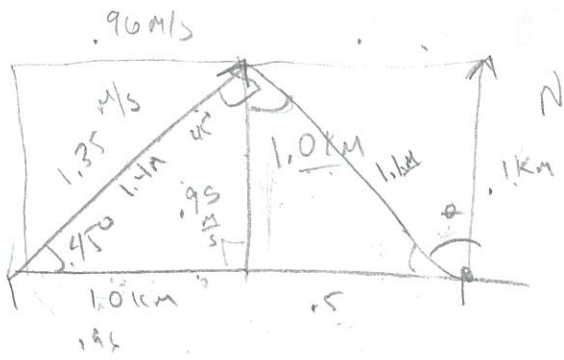
$T = \Delta x = 6.20\text{cm}$

c) increase w/ time

(x component of the velocity continuously increases in the negative direction)

$y = 6.2 \text{ m/s}$

6.



$$\theta = \tan^{-1} \left[ \frac{.5}{1.0} \right] = 26.6^\circ$$

$$V_2 = \frac{1.4 \text{ m}}{1.35 \frac{\text{m}}{\text{s}}} = \frac{1.1 \text{ m}}{x}$$

11 m/s

## Section 4.3

7.

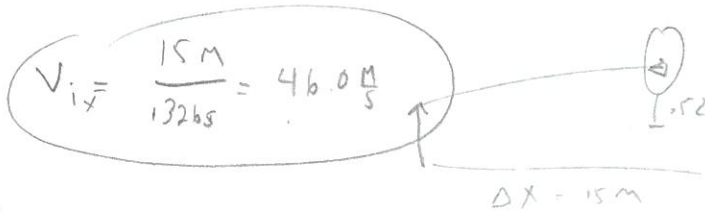
$$\Delta y = \frac{1}{2} g t^2$$

$$\Delta x = 15 \text{ m}$$

$$V_i = ?$$

$$\Delta y = .52 \text{ m}$$

$$t = ?$$



$$V_{ix} = \frac{15 \text{ m}}{.326 \text{ s}} = 46.0 \frac{\text{m}}{\text{s}}$$

$$t = \sqrt{\frac{2 \Delta y}{g}} =$$

$$t = .326 \text{ sec}$$

8.

$$\Delta y = 108 \text{ m}$$

$$V_{ix} = 3.60 \frac{\text{m}}{\text{s}}$$

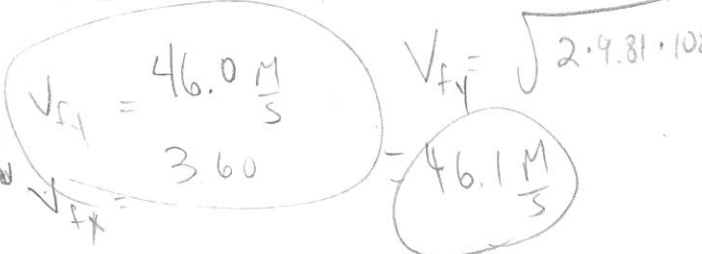
$$V_{fy} = ?$$

$$g = -9.81 \frac{\text{m}}{\text{s}^2}$$

$$t = ?$$

$$t = \sqrt{\frac{2 \cdot 108}{-9.81 \frac{\text{m}}{\text{s}^2}}} = 4.7 \text{ s}$$

$$V_{fy}^2 = V_{iy}^2 + 2g \Delta y$$



$$V_{fy} = \sqrt{2 \cdot 9.81 \cdot 108} = 46.1 \frac{\text{m}}{\text{s}}$$

$$V_f = \sqrt{3.60^2 + 46.1^2} = 46.0 \frac{\text{m}}{\text{s}}$$

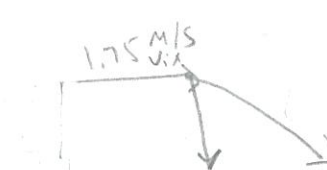
9.

$$V_{ix} = 1.75 \text{ m/s}$$

$$\Delta y = 3.00 \text{ m}$$

$$V_f = ?$$

$$t = .78 \text{ s}$$



$$V_{fy}^2 = V_{iy}^2 + 2g \Delta y$$

$$V_f = \sqrt{2 \left( 9.81 \frac{\text{m}}{\text{s}^2} \right) 3.00 \text{ m}}$$

$$V_{fy} = 7.67 \text{ m/s}$$

$$V_f = \sqrt{1.75^2 + 7.67^2} = 7.87 \frac{\text{m}}{\text{s}}$$

11.  $\Delta x = 18 \text{ m}$   $V_i = \frac{\Delta x}{T} = \frac{32 \text{ m}}{s} = \frac{18 \text{ m}}{T}$   $t = .56 \text{ s}$

$V_i = 32 \frac{\text{m}}{\text{s}}$

$\Delta y = ?$   $\Delta y = \frac{1}{2} g t^2 \Rightarrow = .5 \cdot 9.81 \cdot .56^2$

a)  $\Delta y = 1.5 \text{ m}$

b) gets shorter

c) decreases

13.  $V_i = 2.70 \frac{\text{m}}{\text{s}}$   
 $t = 2.10 \text{ s}$

$\Delta x = 5.67 \text{ m}$

or  $V_{fy} = V_i + g t^2$   
 $20.6 \text{ m/s}$

a)  $V_{ix} = ?$  (2.70 m/s)

b)  $V_i$

$\Delta y = \frac{1}{2} 9.81 \text{ m/s}^2 \cdot (2.10 \text{ s})^2$   
 $21.6 \text{ m}$

$V_{fy}^2 = V_i^2 + 2g \Delta y$

$V_{fy} = 20.6 \text{ m/s}$

c) y - stays the same

x - increase

16.  $\Delta y = 9.0 \text{ m}$   
 $\Delta x = 3.5 \text{ m}$   
 $V_i = ?$

$t = \sqrt{\frac{2 \Delta y}{g}} = 1.45 \text{ s}$

$V_i = \frac{3.5 \text{ m}}{1.45} = 2.5 \frac{\text{m}}{\text{s}}$

$V_{fy} = V_i + g t$

$V_i = 3.3 \frac{\text{m}}{\text{s}}$

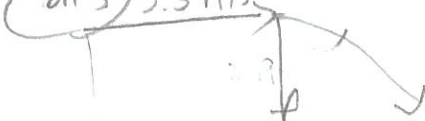
17.

$\theta = 7.66^\circ$

$V_f = ?$   $8.1 \frac{\text{m}}{\text{s}}$   $3.3 \text{ m/s}$

a) .75 s later =  $7.4 \frac{\text{m}}{\text{s}}$

$\tan \theta = \frac{-7.4}{-3.3}$



20.  $169 \text{ m}$

$\Delta y = 5555 \text{ ft} \left( \frac{12''}{1 \text{ ft}} \right) \left( \frac{254 \text{ cm}}{1 \text{ m}} \right) \left( \frac{1 \text{ m}}{1000 \text{ ft}} \right)$

$V_i = 5.0 \frac{\text{m}}{\text{s}}$

$\Delta x = ?$

$t = \sqrt{\frac{2 \cdot 169}{9.81}} = 5.9 \text{ s}$

$\Delta x = V_{ix} T =$

$29.5 \text{ m}$

# Sec. 4.4

23.  $v_i = 17.0 \text{ m/s}$   
 $\theta = 35^\circ$

a)  $13.9 \frac{\text{m}}{\text{s}} = v_i \cos \theta =$



b)  $t = ?$   
 $9.75 \text{ m/s}$   
 $v_f = 9.75 \text{ m/s}$   
 $v_i = 9.75 \text{ m/s}$

$= v_i \sin \theta$   
 $g = \frac{v}{t} \quad \frac{v}{g}$   
 $= \frac{9.75 \text{ m/s}}{9.81 \text{ m/s}^2} = 9.75 \text{ m/s}$   


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 $= 9.81 \text{ m/s}$

$t = 1.94 \text{ s}$

24.  $y = 9.75 \text{ m/s} \downarrow$

$v_i \sin \theta = v_{y_i} = v_{y_f}$

26.  $v_i = 9.50 \text{ m/s}$   
 $\theta = 25^\circ$   
 $t = ?$

$v_i \sin \theta_{y_i} = 4.01 \text{ m/s}$   
 $v_i \sin \theta_{y_f} = -4.01 \text{ m/s}$   
 so  $a = \frac{\Delta v}{t} = \frac{v_f - v_i}{g} = t$

$t = 1.82 \text{ s}$

31.  $V_i = 30.0 \text{ m/s}$

a)  $V_i = 30.0 \text{ m/s}$



Max length  $\theta = 45^\circ$

$$\text{Range}_{\text{max}} = \frac{V_0^2 \sin \theta}{g} = 91.7 \text{ m}$$



32.  $\Delta y = ?$

$\Delta x = 91.7 \text{ m}$

$V_0 = 30.0 \text{ m/s}$

$t = \text{not re}$

$\Delta y = ?$

$$V_{fy}^2 = V_{iy}^2 + 2g\Delta y$$

at top zero

MAX  $45^\circ$

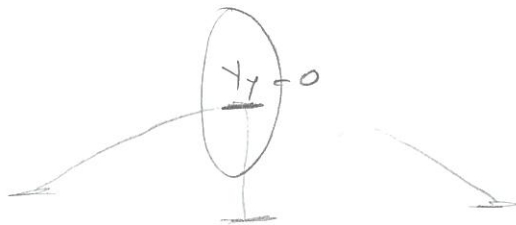
$$V_{iy} \sin \theta = 2g\Delta y$$

$$\Delta y = \frac{(30.0 \text{ m/s} \cdot \sin 45^\circ)^2}{(2 \cdot 9.81)} = 23 \text{ m}$$

# Sec. 4.5

4/0.  $V_i = 12.0 \text{ m/s}$

$\theta = 40^\circ$



$$V_f^2 = (V_i \sin \theta)^2 + 2g\Delta y$$

$$\frac{(-V_i \sin \theta)^2}{2g} = \Delta y$$

$= 3.03 \text{ m}$

45.

$Y = 2.00 \times 10^5 \text{ m}$

$g = 1.80 \text{ m/s}^2$

$V_i = ?$

$V_{f \text{ max}} = 0$   
highest

Max height  $\theta = 45^\circ$

$$V_f^2 = V_i^2 + 2g\Delta y$$

$$V_i = \sqrt{-2g\Delta y} = 848 \frac{\text{m}}{\text{s}}$$

b) Less than bc  $g$  is greater

46.

$g = 9.81 \text{ m/s}^2$

$V_i = 10.2 \text{ m/s}$

$\theta = 25^\circ$

a)  $t_1 = .25$

$t_2 = .50 \text{ s}$

$V_f = ?$

$t_{.25} =$

$t_{.50} =$

X direction does change

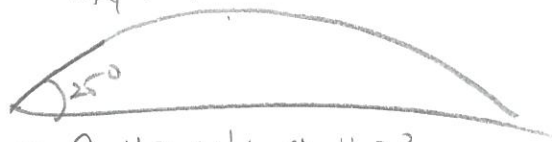
$V_x = V_i \cos \theta = \text{constant}$

$= 9.24 \text{ m/s} \rightarrow$

$t_{.25} \quad V_f = V_0 \sin \theta + gt$

$V_{fy} = 1.86 \text{ m/s}$

$t=.25 \quad \sqrt{9.24^2 + 1.86^2} = 9.42 \text{ m/s } \theta 11.3^\circ$



# General Problems

52.  $V_x = 4.87$   
 $x = 1.95m$

$V_x = \frac{x}{t}$  so  $t = \frac{x}{v}$   
 $t = .40s$   
 $\Delta y = \frac{1}{2}gt^2 = \Delta y = 0.786m$

$\Delta y = h = ?$

59.

$V_i = 11.2 m/s$

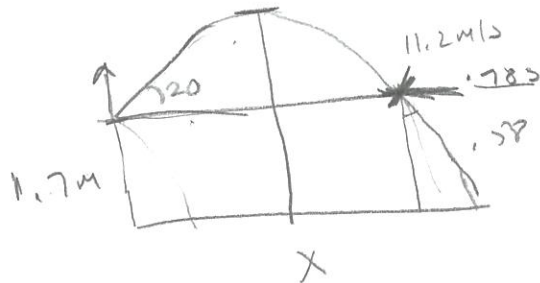
$\theta = 20^\circ$

$h = 5.0' \left( \frac{1m}{3ft} \right) = 1.7m$

$x = ?$

$t = .39s$

$V_{iy} = 3.83 \frac{m}{s}$



Use height to find time  
 $R = \frac{V_i^2 \sin^2 \theta}{g} - h$

$V_f = 0 = 3.83 m/s + gt$

68. a) B)

b)  $V_i =$   
 $\theta = 25^\circ$   
 $x = 35m$

$t = 1.37s = 14.4m$

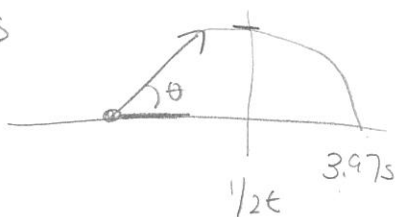
$R = \left( \frac{V_0^2}{g} \right) \sin 2\theta = \text{Range formula}$

$V_0 = \sqrt{\frac{Rg}{\sin 2\theta}} = \sqrt{\frac{35m \cdot 9.81}{\sin 50^\circ}} = 21 m/s$

$x = 35m$

$V_x \cos \theta = \frac{x}{t}$

69.  $V_i = 21.5 m/s$   
 $t = 3.97s$   
 $\theta =$



c)  $t = \frac{x}{V_x \cos \theta} = \frac{35m}{(21 m/s \cdot \cos 25^\circ)}$

$t = 1.8s$

a)  $V_{xi} = \frac{x}{t} = \frac{35m}{3.97}$   
 $+ V_{xi} = 8.8 m/s$

$V_{fy_{top}} = 0 \quad V_f = V_i + gt$

$V_{iy} = g \frac{1}{2} t$

$V_{iy} = 19.4 m/s$

$\theta = \tan^{-1} \left[ \frac{19.4}{8.8} \right] = 66^\circ$



74)  $V_0 \rightarrow$



a)  $t = \sqrt{\frac{2h}{g}}$      $V_0 = \frac{x}{\sqrt{\frac{2h}{g}}}$     so  $V_0 = \frac{w}{\sqrt{\frac{2h}{g}}}$

b)  $V_{0f} = V_{xf}$   
 $V_{yf} = \sqrt{2gh}$      $V_{fy}^2 = \cancel{V_{iy}^2} + 2gh$

$\theta = \tan^{-1} \left[ \frac{y}{x} \right]$

$V_{fy} = \sqrt{2gh}$

So  $\tan^{-1} \left[ \frac{\sqrt{2gh}}{V_0} \right]$